

Giving Key a Vocabulary

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Key is awesome

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\alpha\} \ni \text{names}$

Blake

Angel

Emery

Devon



Key is awesome

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\alpha \ \omega\} \boxplus \text{names}$

Blake 1 7

Angel 2 4 8 9

Emery 3

Devon 5 6



Key is awesome

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\alpha \ \omega \ (\neq \omega)\} \boxplus \text{names}$

| | | | | | |
|-------|---|---|---|---|---|
| Blake | 1 | 7 | | | 2 |
| Angel | 2 | 4 | 8 | 9 | 4 |
| Emery | 3 | | | | 1 |
| Devon | 5 | 6 | | | 2 |



Key: sort?

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\alpha \ \omega \ (\neq \omega)\} \boxtimes \text{names}$

| | | | | | |
|-------|---|---|---|---|---|
| Blake | 1 | 7 | | | 2 |
| Angel | 2 | 4 | 8 | 9 | 4 |
| Emery | 3 | | | | 1 |
| Devon | 5 | 6 | | | 2 |



Key: sort

names \leftarrow \uparrow 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\omega[\Delta\omega;]\} \{\alpha \omega (\neq\omega)\} \exists \text{names}$

| | | | | | |
|-------|---|---|---|---|---|
| Angel | 2 | 4 | 8 | 9 | 4 |
| Blake | 1 | 7 | | | 2 |
| Devon | 5 | 6 | | | 2 |
| Emery | 3 | | | | 1 |



Key: add items?

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\{\omega[\Delta\omega;]\} \{\alpha \omega (\neq\omega)\} \exists \text{names}$

| | | | | | |
|-------|---|---|---|---|---|
| Angel | 2 | 4 | 8 | 9 | 4 |
| Blake | 1 | 7 | | | 2 |
| Colby | | | | | 0 |
| Devon | 5 | 6 | | | 2 |
| Emery | 3 | | | | 1 |



Key: add items

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De
all ← ↑ 'Angel' 'Blake' 'Colby' 'Devon' 'Eme
 $\{\omega[\Delta\omega;]\} \{i \leftarrow^{-1} \downarrow \omega \diamond \alpha \ i \ (\neq i)\} \boxplus \text{names}, \text{all}$

| | | | | | |
|-------|---|---|---|---|---|
| Angel | 2 | 4 | 8 | 9 | 4 |
| Blake | 1 | 7 | | | 2 |
| Colby | | | | | 0 |
| Devon | 5 | 6 | | | 2 |
| Emery | 3 | | | | 1 |



Key: add items, order

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De  
all ← ↑ 'Angel' 'Blake' 'Colby' 'Devon' 'Eme  
{ i ← (1 ↓ ω) - ≠ all } ⋄ α i (≠ i) } ⊞ all; names
```

| | | | | | |
|-------|---|---|---|---|---|
| Angel | 2 | 4 | 8 | 9 | 4 |
| Blake | 1 | 7 | | | 2 |
| Colby | | | | | 0 |
| Devon | 5 | 6 | | | 2 |
| Emery | 3 | | | | 1 |



Key: add items, order, query?

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De  
all ← ↑ 'Colby' 'Emery'  
{i ← (1 ↓ ω) - ≠ all ◊ α i (≠ i)} ⊞ all, names
```

| | | | | |
|-------|---|---|---|---|
| Colby | | | | 0 |
| Emery | 3 | | | 1 |
| Blake | 7 | | | 1 |
| Angel | 4 | 8 | 9 | 3 |
| Devon | 6 | | | 1 |



Key: add items, order, query

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De  
all ← ↑ 'Colby' 'Emery'  
(≠all) ↑ {i ← (1 ↓ ω) - ≠all ◊ α i (≠i)} ⊞ all; names
```

| | | |
|-------|---|---|
| Colby | | 0 |
| Emery | 3 | 1 |



Key: get keys

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De
```

```
(2 = { ≠ ω } ∃ names) ≠ ∪ names
```

Blake

Devon



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

(2 = { ≠ ω } ⊞ names) ≠ ∪ names

Blake

Devon



Key: get keys

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De
```

```
{ ≠ ω } ⊞ names
```

```
2 4 1 2
```



Key: get keys

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De
```

```
{α (≠ω)} ⊞ names
```

```
Blake 2
```

```
Angel 4
```

```
Emery 1
```

```
Devon 2
```



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'Devon'


$\phi\{\alpha (\neq \omega)\} \text{names}$

| | | | |
|-------|-------|-------|-------|
| Blake | Angel | Emery | Devon |
| 2 | 4 | 1 | 2 |



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

↓ $\emptyset\{\alpha (\neq \omega)\}$  names

Blake Angel Emery Devon 2 4 1 2



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$(k \ c) \leftarrow \downarrow \{ \alpha \ (\neq \omega) \} \boxplus \text{names}$

$\uparrow (2=c) \neq k$

Blake

Devon



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$\Rightarrow \{ \uparrow (2 = \omega) \neq \alpha \} / \downarrow \emptyset \{ \alpha (\neq \omega) \} \text{names}$

Blake
Devon



Key: get sorted keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

⇒ {↑ (2=ω) ≠ α} / ↓ ∅ {ω [Ψω;]} {α (≠ω)} ☒ names

Devon
Blake



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

(2 = { ≠ ω } ⊞ names) ≠ ∪ names

Blake

Devon



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

(2 = { ≠ ω } ⊞ names) ≠ voc ← u names

Blake

Devon



Key: get keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$(2 = \{\neq \omega\} \boxtimes \text{voc} \vdash \text{names}) \neq \text{voc} \leftarrow \cup \text{names}$

Blake

Devon



Key: get sorted keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$(2 = \{\neq \omega\} \boxtimes \text{voc} \vdash \text{names}) \neq \text{voc} \leftarrow \{\omega[\Psi \omega;]\} \cup \text{names}$

Devon
Blake



Key: get sorted keys

names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De

$(2 = \{\neq \omega\} \boxtimes \text{voc} \vdash \text{names}) \neq \text{voc} \leftarrow \{\omega[\Psi \omega;]\} \cup \text{names}$

Devon
Blake



What *can* we do with that operand?

{≠ω}☰



What *can* we do with that operand?

$\{\alpha\omega\}$ 

┌ For each unique key:
├ values or key indices
└ key




What *can* we do with that operand?

$\{\alpha\omega\} / \text{voc} \boxplus$

┌ For each unique key:
├ values or key indices
└ key



What *can* we do with that operand?

`voc {αω} .. voc` 

- For each unique key:
 - values or key indices
 - key



What *can* we do with that operand?

$\{\neq\omega\}$ $\cdot\cdot$ voc \boxplus

└ For each unique key:
└ values or key indices



What *can* we do with that operand?

≠^{••} voc



Key: get keys

names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Dev'

(2 = {≠ω} ⊢ names) ≠ u names

| | |
|-------|-------|
| Blake | Devon |
|-------|-------|

≠ ·· voc ⊢



Key proposal: get keys

names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Dev'

$(2 = \{\neq \omega\} \boxplus \text{names}) \neq \cup \text{names}$

| | |
|-------|-------|
| Blake | Devon |
|-------|-------|

$(2 = \neq \text{voc} \boxplus \text{names}) \neq \text{voc} \leftarrow \cup \text{names}$

| | |
|-------|-------|
| Blake | Devon |
|-------|-------|



Key proposal: get sorted keys

names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Devon'

$\{\omega[\Psi\omega]\} (2 = \{\neq\omega\} \boxplus \text{names}) \neq \cup \text{names}$

| | |
|-------|-------|
| Devon | Blake |
|-------|-------|

$(2 = \neq \text{voc} \boxplus \text{names}) \neq \text{voc} \leftarrow \cup \text{names}$

| | |
|-------|-------|
| Blake | Devon |
|-------|-------|



Key proposal: get sorted keys

names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Dev'

~~$\{\omega[\Psi\omega]\} \cup (2 = \{\neq\omega\} \boxminus \text{names}) \neq \cup \text{names}$~~

| | |
|-------|-------|
| Devon | Blake |
|-------|-------|

$(2 = \neq \text{voc} \boxminus \text{names}) \neq \text{voc} \leftarrow \{\omega[\Psi\omega]\} \cup \text{names}$

| | |
|-------|-------|
| Devon | Blake |
|-------|-------|



Key proposal: query

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De  
all ← ↑ 'Colby' 'Emery'  
(≠all) ↑ {i ← (1 ↓ ω) - ≠all ◊ α i (≠i)} ⊞ all; names
```

| | | |
|-------|---|---|
| Colby | | 0 |
| Emery | 3 | 1 |



Key proposal: query

```
names ← ↑ 'Blake' 'Angel' 'Emery' 'Angel' 'De  
all ← ↑ 'Colby' 'Emery'  
(≠all) ↑ {i ← (1 ↓ ω) - ≠all ◊ α i (≠i)} ⊞ all; names
```

Colby 0

Emery 3 1

```
↑(↓all) {α ω (≠ω)} ``all ⊞ names
```

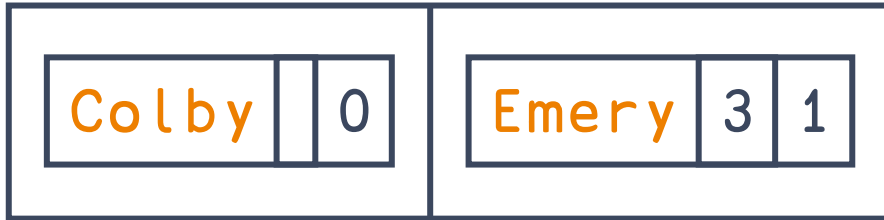
Colby 0

Emery 3 1

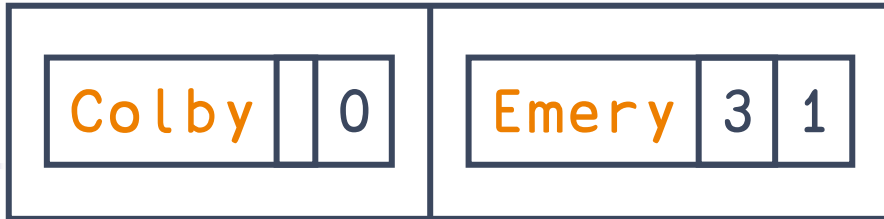


Key proposal: query

names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Dev'
 all ← 'Colby' 'Emery'
 (\neq all) \uparrow { $i \leftarrow (1 \downarrow \omega) - \neq$ all $\diamond c \alpha i (\neq i)$ } \boxplus all; name

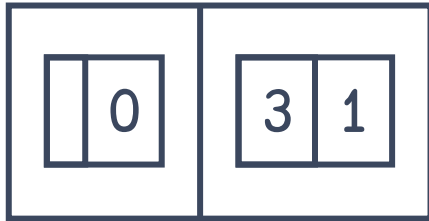


all { $\alpha \omega (\neq \omega)$ } \boxplus all; names

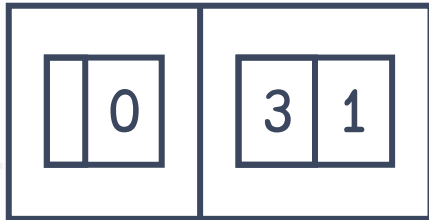


Key proposal: query

```
names ← 'Blake' 'Angel' 'Emery' 'Angel' 'Dev'  
all ← 'Colby' 'Emery'  
(≠all) ↑ {i ← (1 ↓ ω) - ≠all ◊ c_i (≠i)} ⊔ all, names
```



$\{\omega (\neq \omega)\} \cdot \text{all} \sqcup \text{names}$



Giving Key a Vocabulary

Function Operand

`Fm`  `vals`

`Fd`  `vals`

`keys` `Fm`  `vals`

`keys` `Fd`  `vals`

Array Operand

`voc`  `vals`

`voc`  `vals`

`keys(voc`  `)vals`

`keys(voc`  `)vals`



DRAFT PROPOSAL

Giving Key a Vocabulary

Function Operand

`Fm` `vals`

`Fd` `vals`

`keys` `Fm` `vals`

`keys` `Fd` `vals`

Array Operand

`Fm` `voc` `vals`

`voc` `Fd` `voc` `vals`

`Fm` `keys(voc)` `vals`

`voc` `Fd` `keys(voc)` `vals`

`]get is.gd/KeyVoc:aplo`

