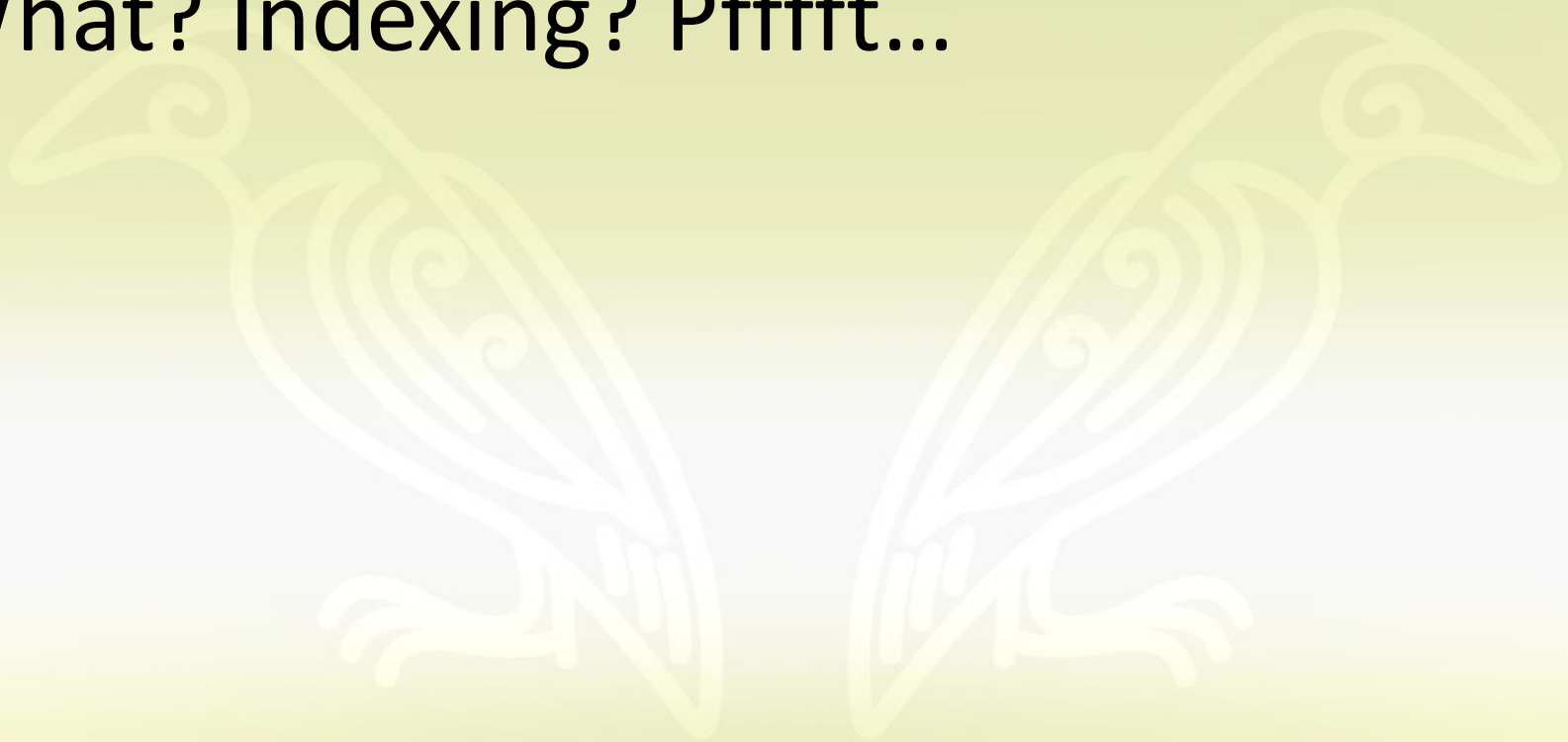


Selecting from Arrays

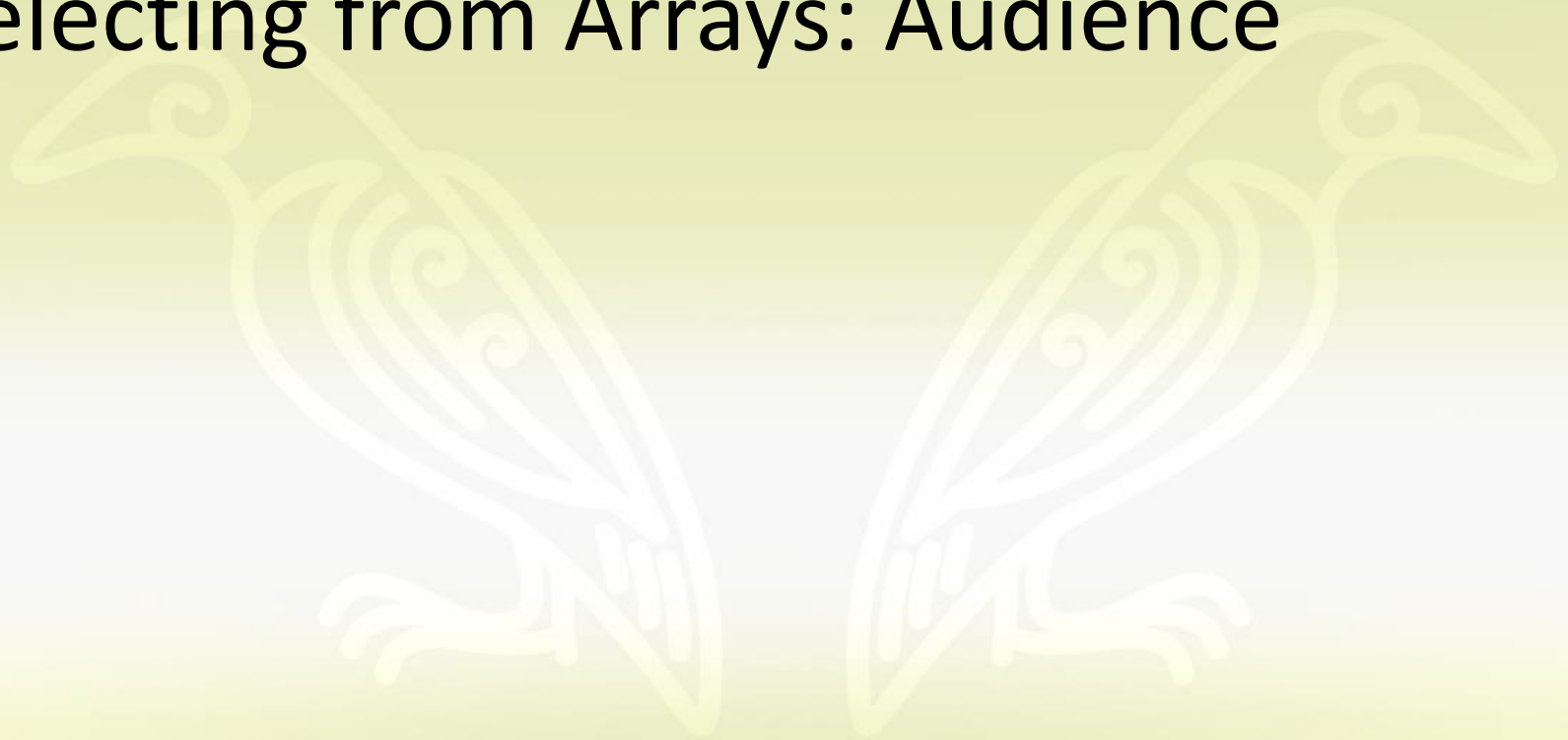
Richard Park (16/04/2020)



What? Indexing? Pffftt...



Selecting from Arrays: Audience



Selecting from Arrays: Audience

Mainly beginners

Selecting from Arrays: Audience

Mainly beginners

Experienced APLers also

Simple

Choose

Reach

The rank operator \circ

Sane

Select

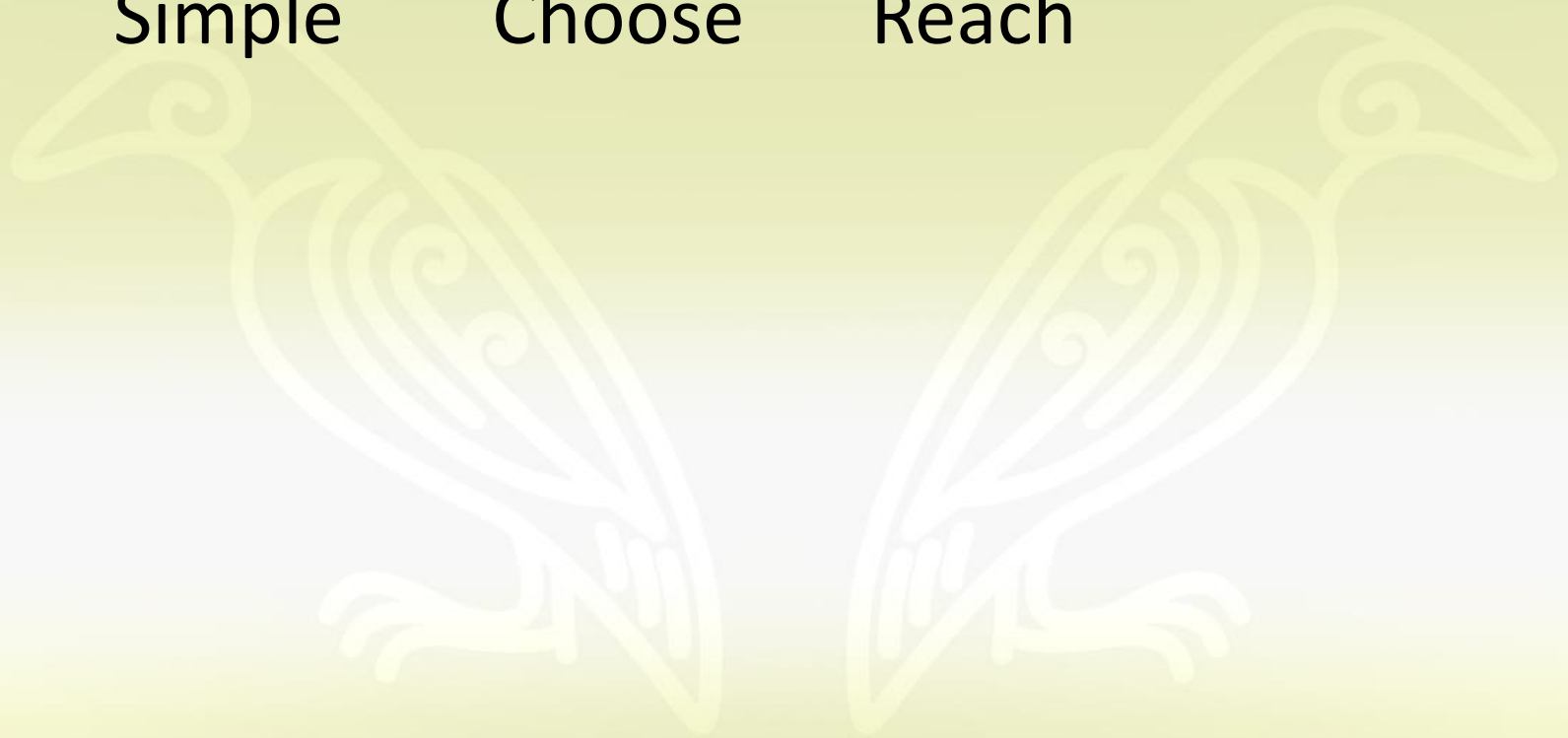
Choose

Cells

Simple

Choose

Reach



Simple

Choose

Reach

Indexed assignment

```
A ← 'YEAST' ♦ A[3 4] ← 'E'
```


Simple

Choose

Reach

Indexed assignment

```
A ← 'YEAST' ⋄ A[3 4] ← 'E'
```

Modified assignment

```
A ← 1 9 ⋄ A[1] +← 5
```

Simple

Choose

Reach

Indexed assignment

```
A ← 'YEAST' ⋄ A[3 4] ← 'E'
```

Modified assignment

```
A ← 1 9 ⋄ A[1] +← 5
```

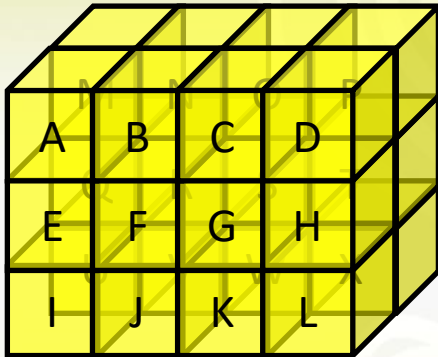
Optimised

Cells, subarrays and elements

A ← 2 3 4 ρ □ A

3D Array

Dimensions / Axes

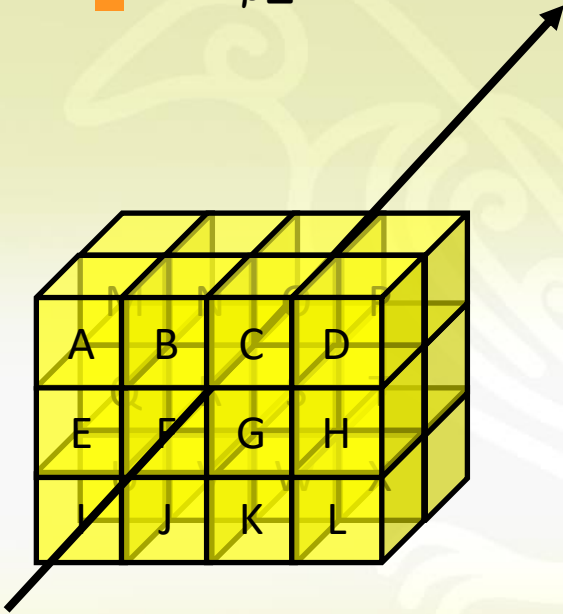


Cells, subarrays and elements

A ← 2 3 4p A

3D Array

Dimensions / Axes

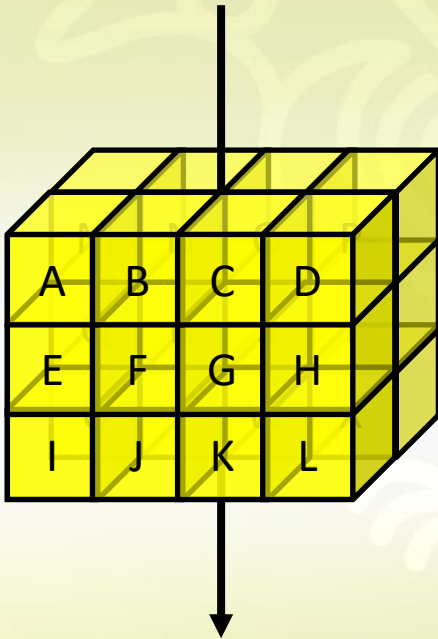


Cells, subarrays and elements

A ← 2 3 4p A

3D Array

Dimensions / Axes

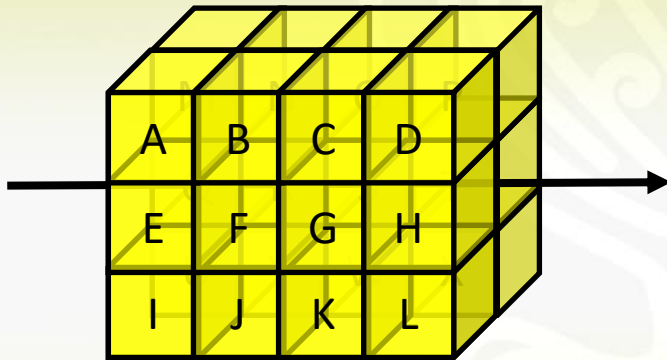


Cells, subarrays and elements

A ← 2 3 4 □ A

3D Array

Dimensions / Axes

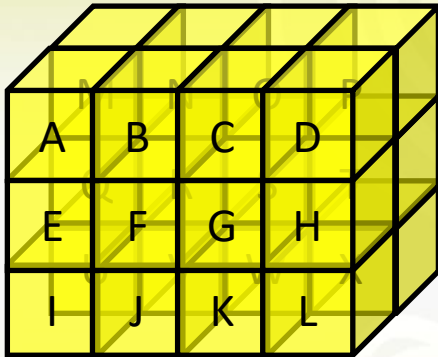


Cells, subarrays and elements

A ← 2 3 4p A

3D Array

Major cell: Matrix

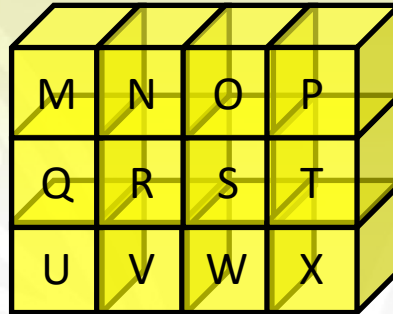
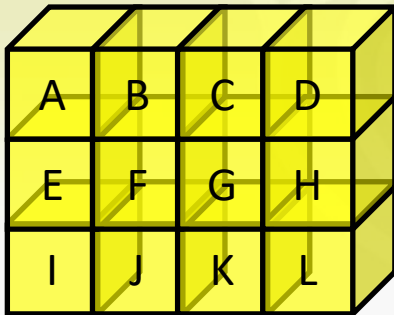


Cells, subarrays and elements

A ← 2 3 4p A

3D Array

Major cell: Matrix

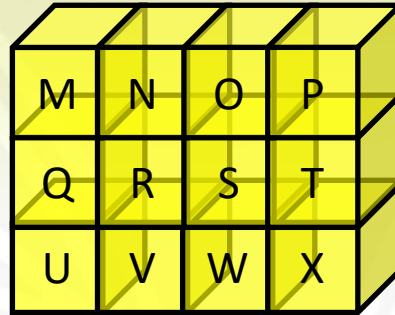
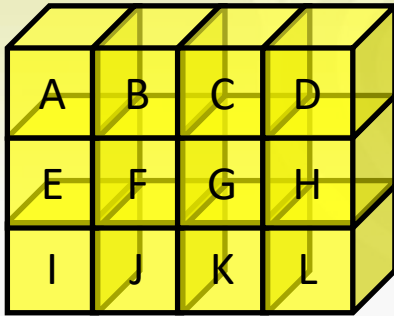


Cells, subarrays and elements

A ← 2 3 4p A

3D Array

Major cell: Matrix



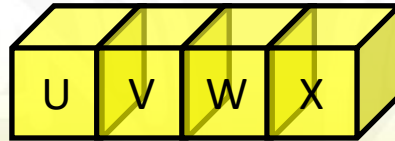
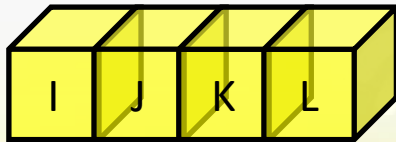
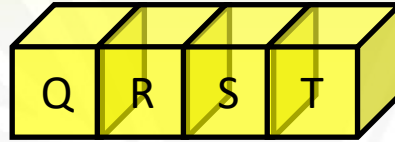
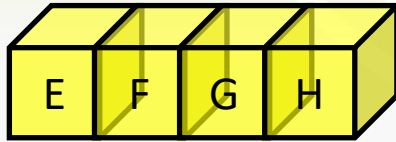
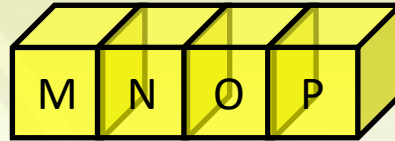
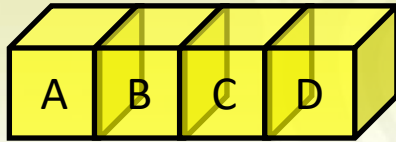
Cells, subarrays and elements

A ← 2 3 4p A

3D Array

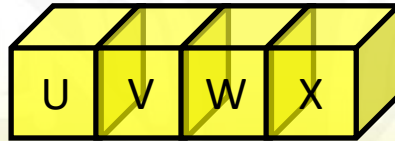
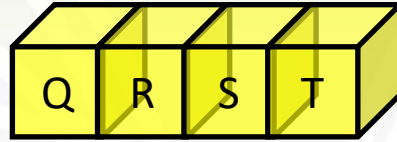
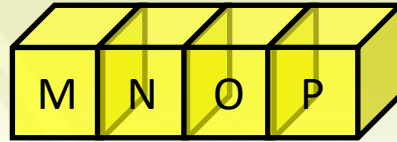
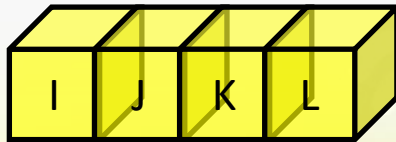
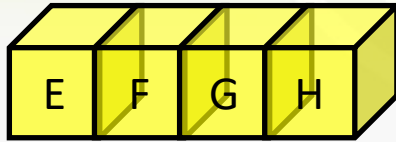
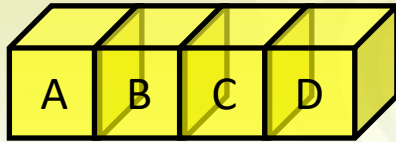
Major cell: Matrix

1-cell: Vector



Cells, subarrays and elements

A ← 2 3 4 ρ A



3D Array

Major cell: Matrix

1-cell: Vector

0-cell: Scalar

Cells, subarrays and elements

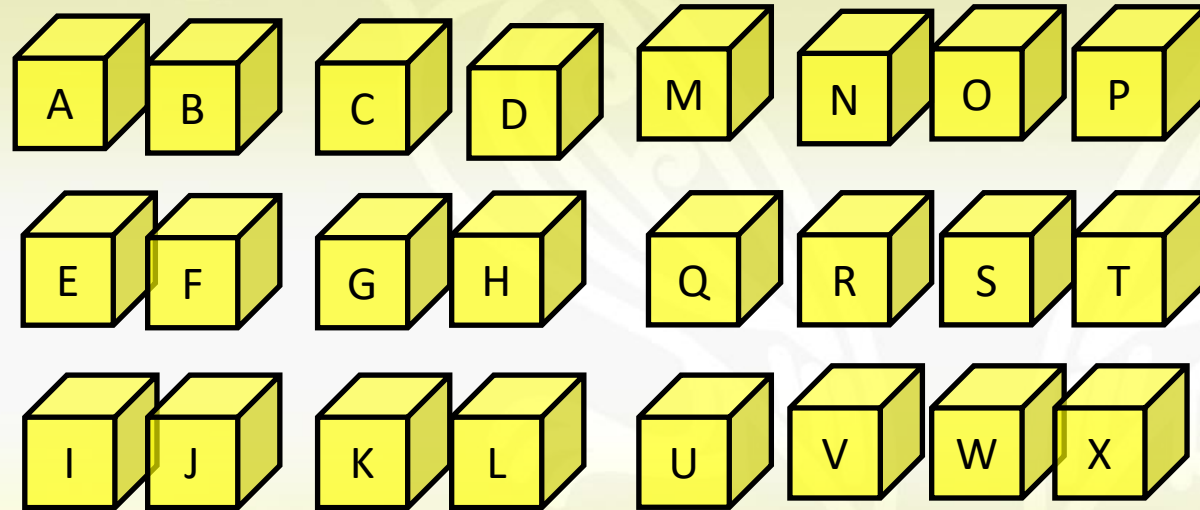
A ← 2 3 4 ρ A

3D Array

Major cell: Matrix

1-cell: Vector

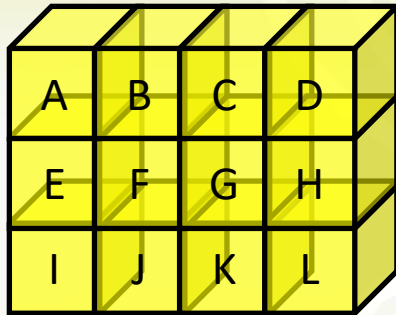
0-cell: Scalar



Simple indexing

A ← 2 3 4 ρ A
A[1;;]

ABCD
EFGH
IJKL

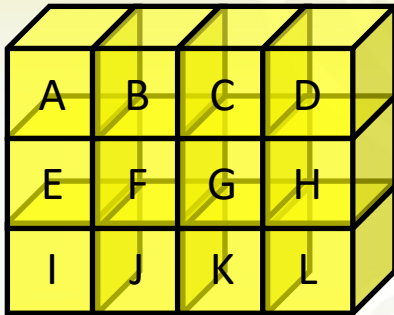


A	B	C	D
E	F	G	H
I	J	K	L

Simple indexing

A ← 2 3 4 p A
1 A

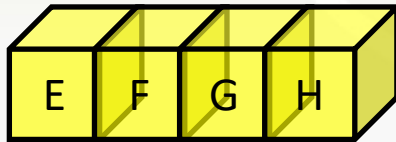
ABCD
EFGH
IJKL



A	B	C	D
E	F	G	H
I	J	K	L

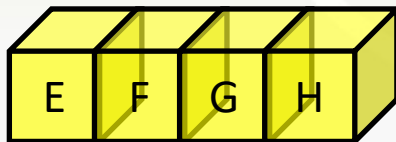
Simple indexing

A ← 2 3 4 ρ A
A[1;2;]
EFGH



Simple indexing

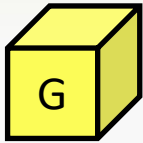
A ← 2 3 4ρA
1 2A
EFGH



Simple indexing

A ← 2 3 4 ρ A
A[1;2;3]

G

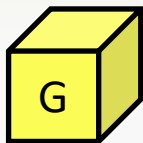


Simple indexing

A ← 2 3 4 ρ A

1 2 3 A

G



Simple indexing

A ← 2 3 4 ρ A

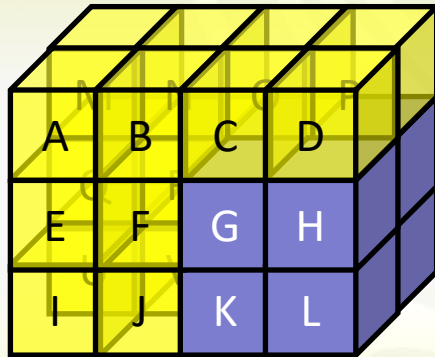
A[1 2; 2 3; 3 4] (1 2)(2 3)(3 4) A

GH

KL

ST

WX



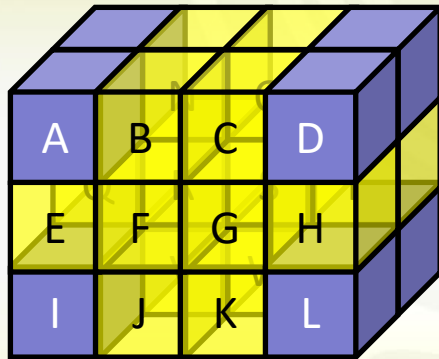
Simple indexing

A ← 2 3 4 ρ A

A[1 2; 1 3; 1 4] (1 2)(1 3)(1 4) A

AD
IL

MP
UX



Simple indexing

	A ← 2 3 4 p A	A[1 2;1 3;1 4]	(1 2)(1 3)(1 4) A
ABCD		AD	
EFGH		IL	
IJKL			
MNOP		MP	
QRST		UX	
UVWX			

Choose indexing

A ← 2 3 4p□A

A[(1 1 1)(2 1 4)(1 3 4)]

ABCD
EFGH
IJKL

APL

MNOP
QRST
UVWX

Choose indexing

A ← 2 3 4p□A

A[(1 1 1)(2 1 4)(1 3 4)]

A B C D
E F G H
I J K L

M N O P
Q R S T
U V W X

APL

Reach indexing

```
nest←2 2 2ρ(2 2ρ'DYAL') 1 2 3 (2 2ρ'ABCD') ('AE' 'IO' 'U') 'NT' 4
```

DY	1
AL	
2	3

AB	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE		IO	U	
CD				
NT	4			

Reach indexing

nest

DY	1
AL	
2	3

AB	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE		IO	U	
CD				
NT	4			

nest[**c 2 1 2**]

AE	IO	U
----	----	---

c 2 1 2

2	1	2
---	---	---

Reach indexing

nest

DY AL	1
2	3

AB CD	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE	IO	U		
NT	4			

nest[**c(2 1 2)2**]

IO

c(2 1 2)2

2	1	2	2
---	---	---	---

Reach indexing

nest

DY	1
AL	
2	3

AB	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE		IO	U	
CD				
NT	4			

0

nest[$c(2\ 1\ 2)2(2)$]

$c(2\ 1\ 2)2(2)$

2	1	2	2	2
---	---	---	---	---

Reach indexing

nest

DY AL	1
2	3

AB CD	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE	IO	U		
NT	4			

DOMAIN ERROR
 $(c(2\ 1\ 2)2(2)) \square nest$
 ^

$c(2\ 1\ 2)2(2)$

2	1	2	2	2
---	---	---	---	---

Pick ~~Reach~~ indexing

nest

DY	1
AL	
2	3

AB	<table border="1"> <tr> <td>AE</td> <td>IO</td> <td>U</td> </tr> </table>	AE	IO	U
AE		IO	U	
CD				
NT	4			

0

$((2\ 1\ 2))2(2) \Rightarrow \text{nest}$

$(2\ 1\ 2)2(2)$

2	1	2	2	2
---	---	---	---	---

Pick ~~Reach~~ indexing

```
□←'this' 'that' 'the other thing'
```

this	that	the other thing
------	------	-----------------

```
3>'this' 'that' 'the other thing'  
the other thing
```

Simple

Choose

Reach

Simple **Subarrays**

Choose

Reach

Simple **Subarrays**

Choose **0-cells AKA Scalars**

Reach

Simple **Subarrays**

Choose **0-cells AKA Scalars**

Reach **Nested arrays**

Squad □

A ← 2 3 4 ρ □ A

ABCD

EFGH

IJKL

MNOP

QRST

UVWX

Squad □

Indexing as a function ∴ you can use operators

A←2 3 4ρ□A

ABCD

EFGH

IJKL

MNOP

QRST

UVWX

Squad ☐

Indexing as a function ∴ you can use operators

$A \leftarrow 2 \ 3 \ 4 \rho \square A$

$2 \square \circ 2 \vdash A$

$2 \square [2] A$

ABCD

EFGH

EFGH

QRST

IJKL

MNOP

QRST

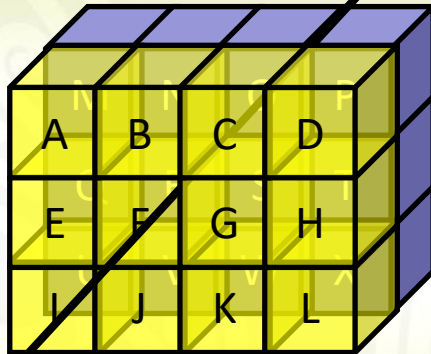
UVWX

Squad with axis $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$

A ← $\begin{bmatrix} 2 \\ 3 \\ 4 \end{bmatrix} \rho \begin{bmatrix} 1 \\ 2 \end{bmatrix} A$

$\begin{bmatrix} 2 \\ 3 \\ 4 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} A$

MNOP
QRST
UVWX

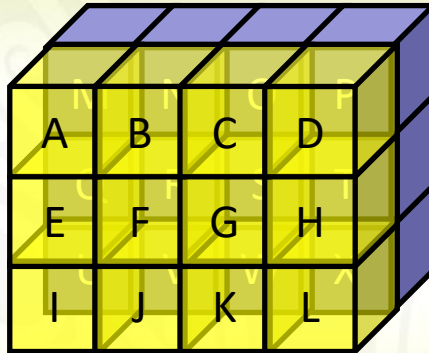


Squad with rank $\begin{bmatrix} 0 \\ 0 \end{bmatrix}$

$$A \leftarrow \begin{bmatrix} 2 & 3 & 4 \end{bmatrix} \rho \begin{bmatrix} 1 \\ 1 \end{bmatrix} A$$

$$\begin{bmatrix} 2 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 3 \end{bmatrix} \vdash A$$

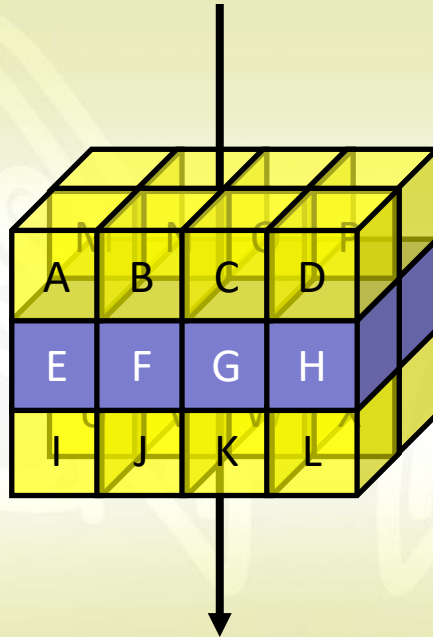
MNOP
QRST
UVWX



Squad with axis `[] []`

A ← 2 **3** 4ρ[]A

2[] [**2**]A
 EFGH
 QRST



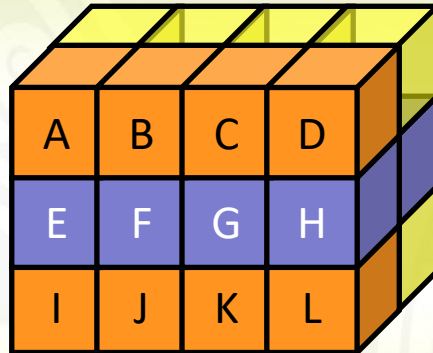
Squad with rank $\begin{bmatrix} & \\ & \end{bmatrix}$

A ← $\begin{bmatrix} & \\ & \end{bmatrix}$ 3 4 $\rho \begin{bmatrix} & \\ & \end{bmatrix}$ A

$\begin{bmatrix} & \\ & \end{bmatrix}$ $\begin{bmatrix} & \\ & \end{bmatrix}$ A

EFGH

QRST



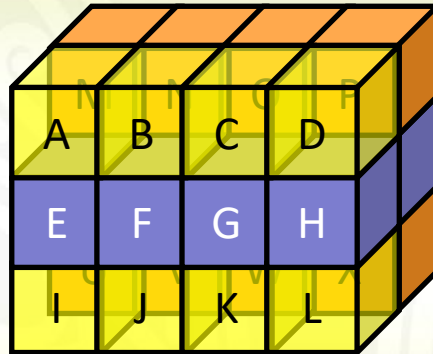
Squad with rank $\begin{bmatrix} 2 & 2 \end{bmatrix}$

$A \leftarrow \begin{bmatrix} 2 & 3 & 4 \end{bmatrix} \rho \begin{bmatrix} 2 & 2 \end{bmatrix} A$

$\begin{bmatrix} 2 & 2 \end{bmatrix} \begin{bmatrix} 2 & 2 \end{bmatrix} \vdash A$

EFGH

QRST



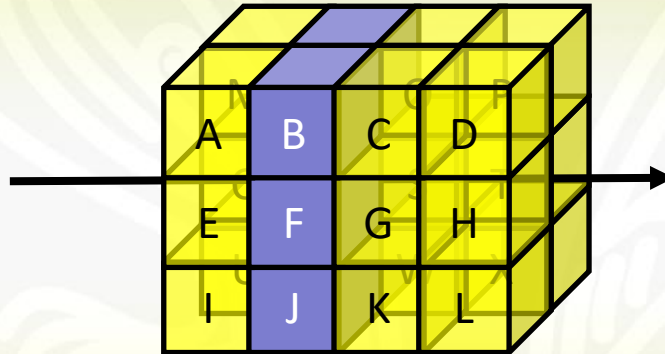
Squad with axis $[[[]]]$

A ← 2 3 4 ρ A

2 $[[[]]]$ 3 A

BFJ

NRV



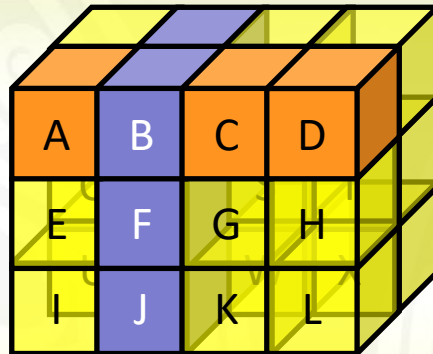
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 ρ A

2 $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ 1 A

BFJ

NRV



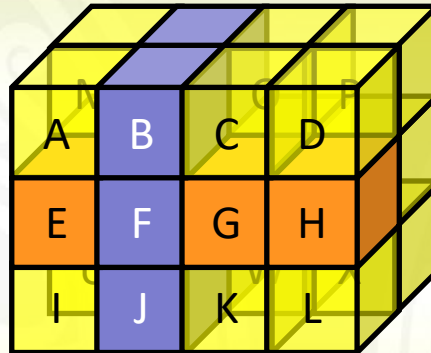
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 $\rho \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

$\begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

BFJ

NRV



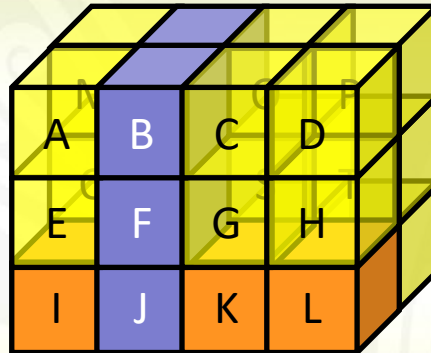
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 ρ A

2 $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ 1 A

BFJ

NRV



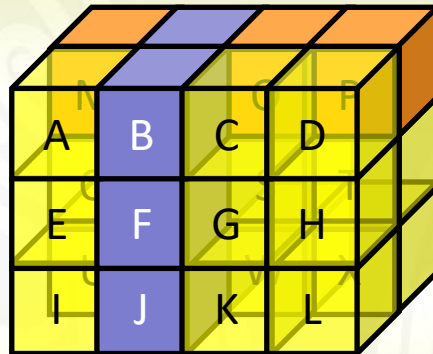
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 $\rho \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

$\begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

BFJ

NRV



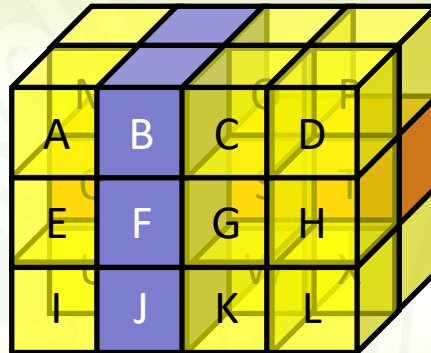
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 $\rho \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

$\begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

BFJ

NRV



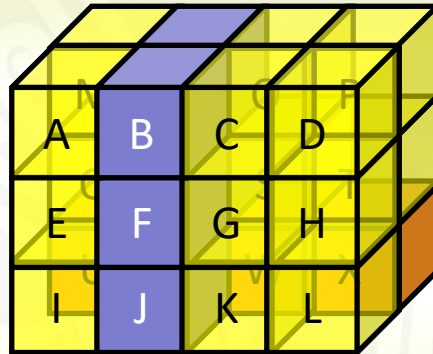
Squad with rank $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

A ← 2 3 4 $\rho \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

$\begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$

BFJ

NRV



Squad with rank 0

`⊖←n←⊘3 5ρι15` `1 3 4⊖0 2←n`

```
1  6 11
2  7 12
3  8 13
4  9 14
5 10 15
```

```
1  6 11
3  8 13
4  9 14
```

Squad with rank 0

```

n←3 5 ρι 15      1 3 4 0 99←n

```

1	6	11	1	6	11
2	7	12	3	8	13
3	8	13	4	9	14
4	9	14			
5	10	15			

"Sane" indexing

$I \leftarrow \boxed{\cdot} 0 \ 99$

$\boxed{\cdot} \leftarrow n \leftarrow \boxed{\cdot} 3 \ 5 \rho \iota 15$

1	6	11
2	7	12
3	8	13
4	9	14
5	10	15

"Sane" indexing

$I \leftarrow \{0 \dots 99\}$

$\{ \leftarrow n \leftarrow \{3 \dots 15\}$

$(\{1 \ 3 \ 4\}) \{n\}$ A "Insane"

1	6	11
2	7	12
3	8	13
4	9	14
5	10	15

1	6	11
3	8	13
4	9	14

"Sane" indexing

$I \leftarrow \{0 \dots 99\}$

$\{ \leftarrow n \leftarrow \{3 \dots 15\}$

$(\{1 \ 3 \ 4\}) \{n\}$ A "Insane"

1 6 11

1 6 11

2 7 12

3 8 13

3 8 13

4 9 14

4 9 14

1 3 4 I n

5 10 15

1 6 11

3 8 13

4 9 14

"Sane" indexing

$I \leftarrow \boxed{0} 99$

$\boxed{0} \leftarrow n \leftarrow 3 \ 5 \rho \iota 15$

1 6 11
2 7 12
3 8 13
4 9 14
5 10 15

1 3 4 I n

1 6 11
3 8 13
4 9 14
1 6 11
3 8 13
4 9 14

1 0 1 1 0 \neq n

"Sane" indexing

'APPLE'[1 3 4] a Intuitive, beginner friendly
APL
1 0 1 1 0/'APPLE' a Booleans
APL

"Sane" indexing

```
1 3 4 I 'APPLE'      A Sane  
APL
```

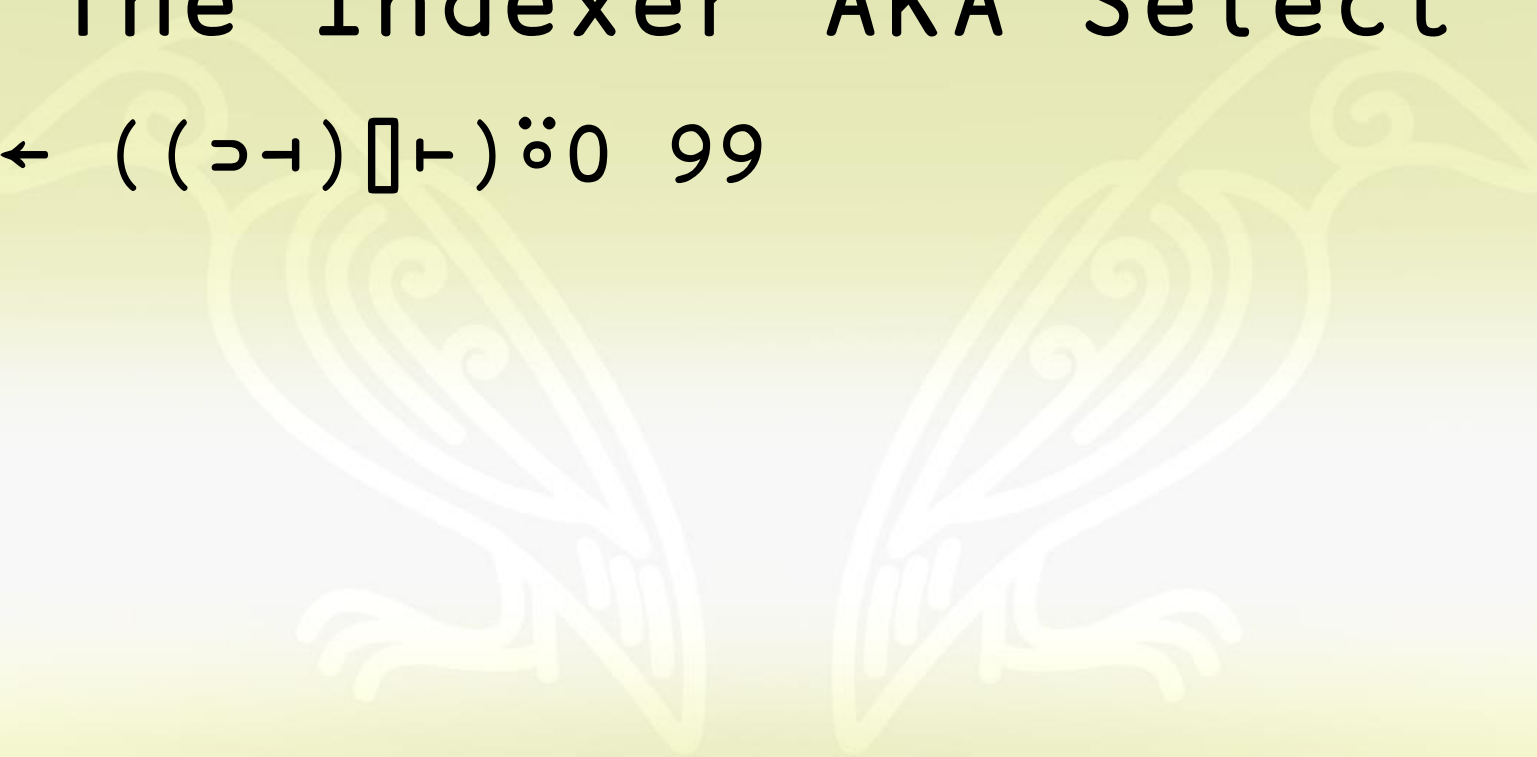


"Sane" indexing

```
1 3 4 I 'APPLE'      ρ Sane
APL
1 0 1 1 0 ≠ 'APPLE'  ρ Rank polymorphic
APL
```

The Indexer AKA Select

```
I ← ((⊃←)[]⊢)∘0 99
```



The Indexer AKA Select

```
I ← ((⊃←)⊠←)⊘0 99
```

```
1 I A      1⊠A      A[1;;]      1⊠⊘0 99←A
```

```
ABCD
```

```
EFGH
```

```
IJKL
```

The Indexer AKA Select

`I ← ((⊃←)⊂←)∘0 99`

`⊂←A←2 3 4ρ⊂A (1 2)(2 3) I A`

ABCD

EFGH

IJKL

EFGH

UVWX

`A[(1 2, 2 3)∘.,⊂4]`

MNOP

QRST

UVWX

EFGH

UVWX

The Indexer AKA Select

$I \leftarrow ((\rightarrow) \square \vdash) \circ 0 \ 99$

$\square \leftarrow A \leftarrow 2 \ 3 \ 4 \rho \square A \quad (1 \ 2 \ 4) (2 \ 3) \ I \ A$

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX

The Indexer AKA Select

I ← ((⊃←)⊂⊆)⊆0 99

⊂←A←2 3 4ρ⊂A

(1 2 4)(2 3) I A

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX



The Indexer AKA Select

$I \leftarrow ((\rightarrow) \square \vdash) \circ 0 \ 99$

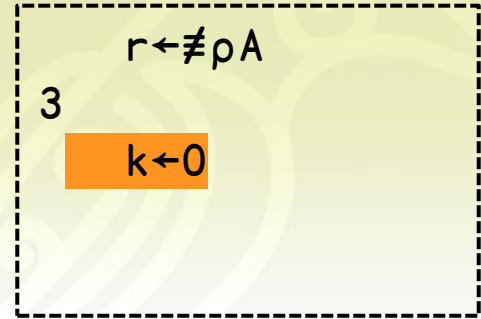
$\square \leftarrow A \leftarrow 2 \ 3 \ 4 \rho \square A$

$(1 \ 2 \ 4) (2 \ 3) \ I \ A$

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX



The Indexer AKA Select

I ← ((→←)[]←)ö0 99

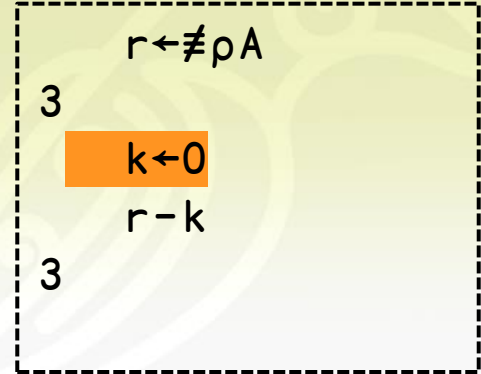
←A←2 3 4ρ←A

(1 2 4)(2 3) I A

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX



The Indexer AKA Select

$I \leftarrow ((\rightarrow) \square \vdash) \circ 0 \ 99$

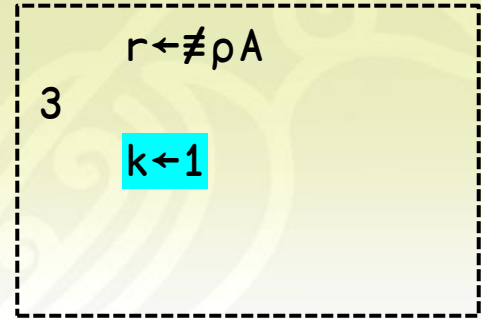
$\square \leftarrow A \leftarrow 2 \ 3 \ 4 \rho \square A$

$(1 \ 2 \ 4) (2 \ 3) \ I \ A$

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX



The Indexer AKA Select

$I \leftarrow ((\rightarrow) \square \vdash) \circ 0 \ 99$

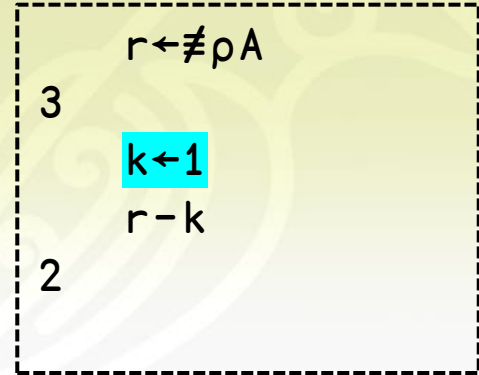
$\square \leftarrow A \leftarrow 2 \ 3 \ 4 \rho \square A$

$(1 \ 2 \ 4) (2 \ 3) \ I \ A$

ABCD
EFGH
IJKL

H
UVWX

MNOP
QRST
UVWX



The Indexer AKA Select

```
I ← ((⊃←)[]⊢)∘0 99
```

```
(1 2 4)(2 3) I A
```

```
H
```

```
UVWX
```

NB. The "from" verb in J

```
(0 1 3;1 2) { A
```

```
H
```

```
UVWX
```

The Indexer AKA Select

```
I ← ((⊃←)⊠⊢)⊘0 99
      1(1 3)⊠A
```

ABCD

IJKL

NB. The "from" verb in J

```
(<0;0 2) { A
```

ABCD

IJKL

Squad with rank ρ

$\rho \leftarrow A \leftarrow 2 \ 3 \ 4 \rho A \quad (\uparrow(1 \ 1 \ 1)(2 \ 1 \ 4)(1 \ 3 \ 4)) \rho \circ 1 \ 99 \leftarrow A$

ABCD

EFGH

IJKL

APL

MNOP

QRST

UVWX

Squad with rank ρ

$\rho \leftarrow A \leftarrow 2 \ 3 \ 4 \rho A$ $(\uparrow(1 \ 1 \ 1)(2 \ 1 \ 4)(1 \ 3 \ 4)) \rho \circ 1 \ 99 \leftarrow A$
 ABCD APL
 EFGH Choose $\leftarrow \rho \circ 1 \ 99$
 IJKL

 MNOP
 QRST
 UVWX

Squad with rank 0

←A←2 3 4ρA

3 99 2-A

ABCD

IJKL

EFGH

UVWX

IJKL

Cells ← 99 k

MNOP

QRST

UVWX

Squad with rank 00

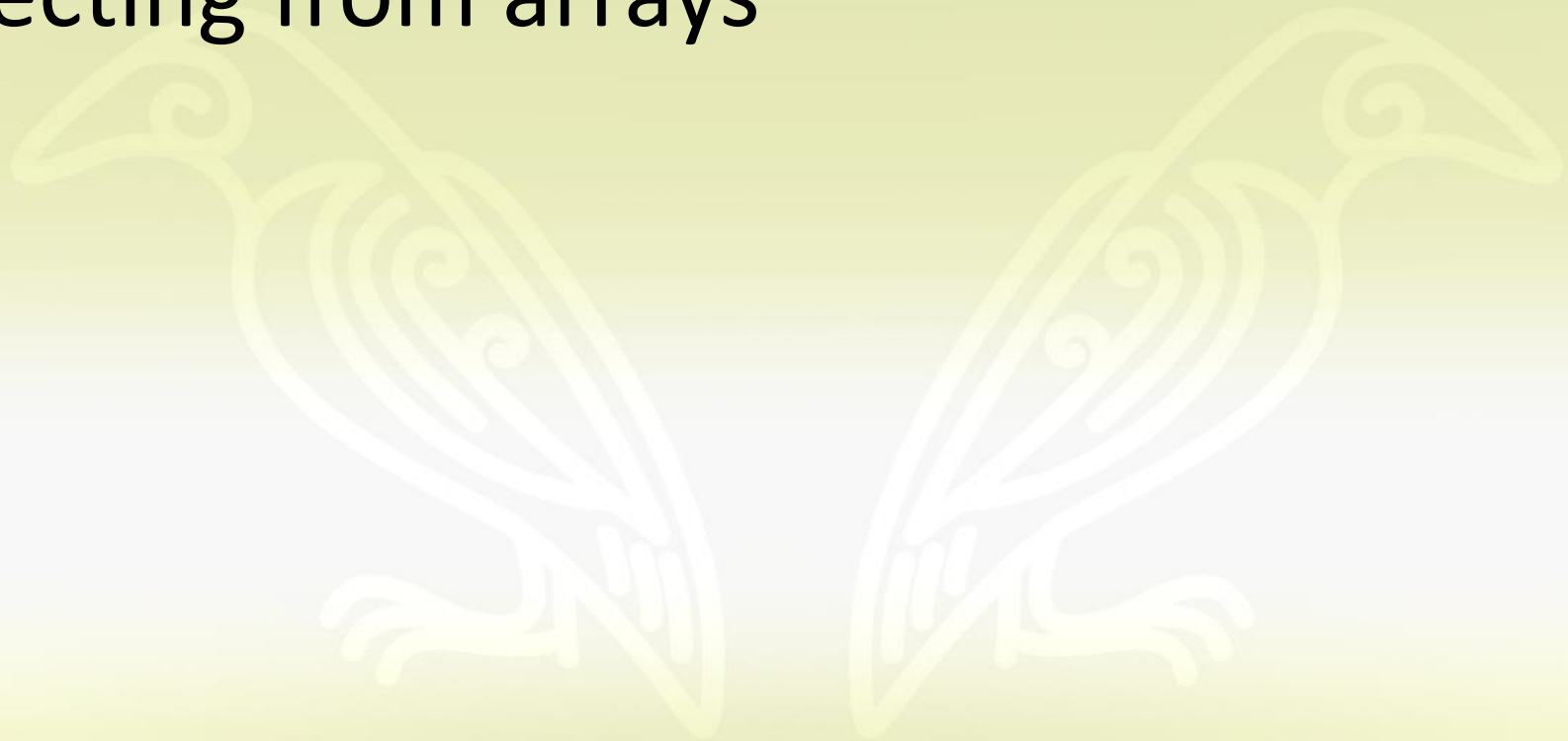
0 ← A ← 2 3 4 ρ 0 A 3 3 0099 2 ← A
 ABCD KW
 EFGH
 IJKL
 MNOP
 QRST
 UVWX
 Cells ← 0099 k

Squad with rank 0

$\leftarrow A \leftarrow 2 \quad 3 \quad 4 \rho \leftarrow A$
(c 2 3) 0 99 2 ← A

ABCD	EFGH
EFGH	IJKL
IJKL	
	QRST
MNOP	UVWX
QRST	
UVWX	Cells ← 0 99 k

Selecting from arrays



Selecting from arrays

[]



Selecting from arrays

```
[ ]
```

```
[]
```

Selecting from arrays

```
[ ]
```

```
[]
```

```
⋈
```

Selecting from arrays

```
[ ]
```

```
[]
```

```
>
```

```
[][]
```

Selecting from arrays

[]

[]

⊃

[] []

[] ⋄

Selecting from arrays

```
[ ] I ← [0 99] a Sane
```

```
[
```

```
>
```

```
[ ]
```

```
[0
```

Selecting from arrays

```
[ ] I ← ⍳0 99 ⍵ Sane
```

```
⍵ I ← ((⊃⊆)⍵)⍳0 99
```

```
⊃
```

```
⍵[ ]
```

```
⍵⍳
```

Selecting from arrays

[] I ← [0 99] a Sane

[] I ← ((→) [←]) 0 99

↳ Choose ← [1 99]

[]

[0]

Selecting from arrays

```

[ ]      I ← [0 99] ⍲ Sane
[ ]      I ← ((⊃⊣) [⊣]) ⍲ 99
⊃        Choose ← [1 99]
[ ]      Cells ← [k]
[ ]
[ ]

```

Performance



Performance

Pre v18.0

100 k

Performance

Pre v18.0

100 k

New in v18.0

100 99

100 99 k

Performance

Pre v18.0

1000 k

New in v18.0

100 99

1000 k

1 = 99α : 1000 k

Indexed assignment

A

ABCD

EFGH

IJKL

MNOP

QRST

UVWX

Indexed assignment

```
A[1 2;1 3;1 4] ← 'ö'
```

öBCö

EFGH

öJKö

öNOö

QRST

öVWö

Search: Indexed assignment

help.dyalog.com

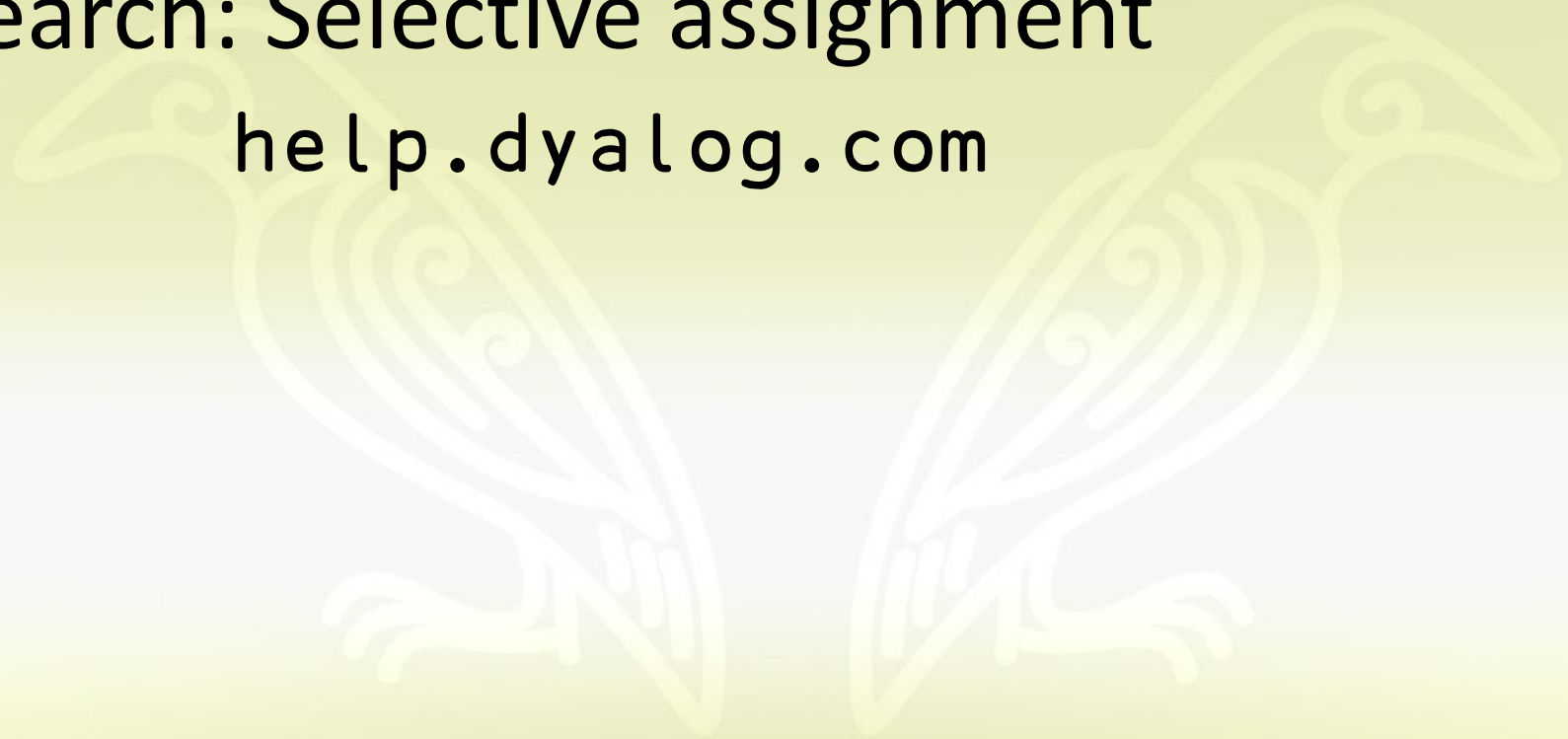
Selective assignment

Functions for Selective Assignment

↑	Take
↓	Drop
,	Ravel
⍒	Table
⊖	Reverse, Rotate
ρ	Reshape
⊃	Disclose, Pick
⊖	Transpose (Monadic and Dyadic)
/f	Replicate
\t	Expand
⍋	Index
ε	Enlist (⍋ML≥1)

Search: Selective assignment

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Merge arrays with @

```
0@(( , 1 3 5 . , 1 3) , (2 4 . , 2))├n
```

```
0 6 0
```

```
2 0 12
```

```
0 8 0
```

```
4 0 14
```

```
0 10 0
```

Merge arrays with @

`-@(2|1)-n`

`-1 6 -11`

`2 -7 12`

`-3 8 -13`

`4 -9 14`

`-5 10 -15`

Selecting from arrays

```
[ ] I ← [0 99] ⍲ Sane
```

```
[ ] I ← ((⊃←) [⊢]) ⍲ 99
```

```
⊃ Choose ← [1 99]
```

```
[ ] Cells ← [k]
```

```
[ ]
```


Next Week: BAA Webinar

Thursday 23rd April **16:00 BST**

Introducing qWC Alpha 0.4 – MJH Software Services

<https://britishaplassociation.org/webinar-schedule-2020/>

Next Dyalog Webinar

Thursday 30th April **16:00 BST**

Introducing Dyalog version 18.0 – Morten Kromberg

dyalog.tv