

User-Defined Operators

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Overview

Why?

What?

How?

Examples



Why define your own operators?

Apply multiple functions in similar ways

Add a parameter to tweak behaviour

Achieve nicer looking expressions

Amend primitives to your needs

Avoid repeating yourself



Why define your own operators?

Apply multiple functions in similar ways

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Avoid repeating yourself

... in ways that isn't part of the core language



What is an operator?

MONADIC
OPERATOR

$F /$

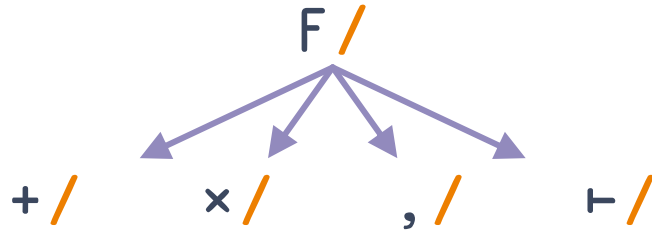
DYADIC
OPERATOR

$F . G$

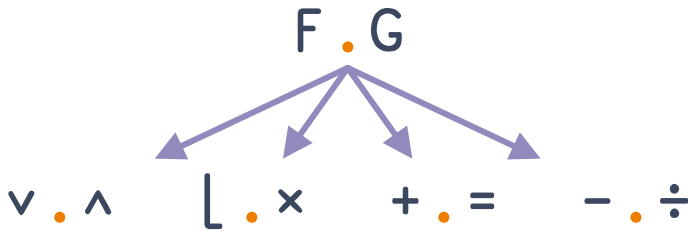


What is an operator?

MONADIC
OPERATOR

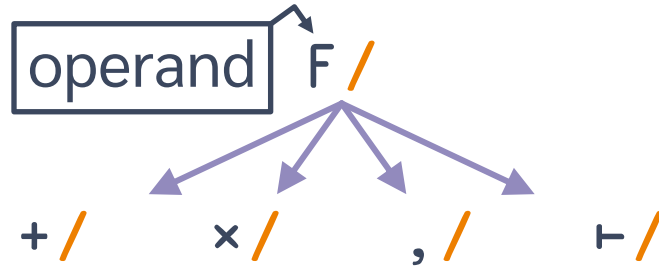


DYADIC
OPERATOR

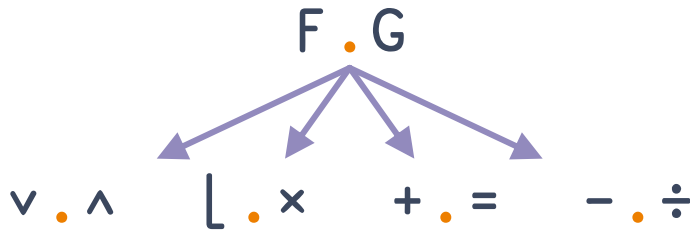


What is an operator?

MONADIC
OPERATOR

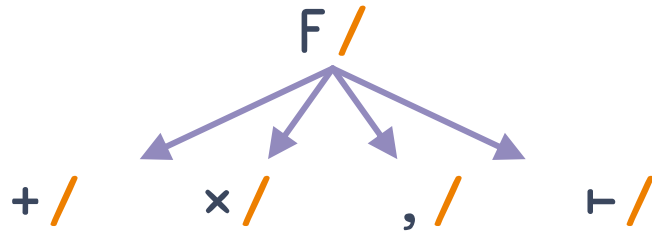


DYADIC
OPERATOR

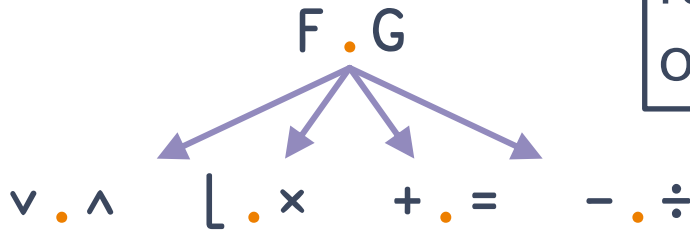


What is an operator?

MONADIC
OPERATOR



DYADIC
OPERATOR



function
operand



What is an operator?

MONADIC
OPERATOR

+ / × ÷ , \ †

DYADIC
OPERATOR

√ • ^ [@ × + * = - ÷ ÷

function
operand



What is an operator?

MONADIC
OPERATOR

42~

1200I

array
operand

DYADIC
OPERATOR

!3

1.+

'Hi' R 'Hello'



What is an operator?

derived
functions

MONADIC
OPERATOR

42  1200I

DYADIC
OPERATOR

1  3 1  + 'Hi '  R 'Hello'



What is an operator?

derived
functions

MONADIC
OPERATOR

Answer ← 42☺

Format ← 1200I

DYADIC
OPERATOR

Replace ← 'Hi' □R 'Hello'

Increment ← 1 ◦ +

Windows ← ⊢ ◊ 3



What is an operator?

derived
functions

MONADIC
OPERATOR

Answer \leftarrow 42 $\ddot{\smile}$

\mathcal{A} ambivalent

Format \leftarrow 1200 \mathbf{I}

\mathcal{A} dyadic

DYADIC
OPERATOR

Replace \leftarrow 'Hi' \square \mathbf{R} 'Hello'

\mathcal{A} ambivalent

Increment \leftarrow 1 \circ +

\mathcal{A} monadic

Windows \leftarrow \vdash \square 3

\mathcal{A} monadic



What is an operator?

derived
functions

MONADIC
OPERATOR

Answer ← 42 😊
Format ← 1200I

an ambivalent

```
'a' Answer 'b'  
42  
Answer 'b'  
42
```

DYADIC
OPERATOR

Replace ← 'Hi ' □ R 'He'
Increment ← 1 ◦ +
Windows ← 1 ◻ 3

an monadic
an monadic



What is an operator?

derived
functions

MONADIC
OPERATOR

Answer ← 42~

⌈ ambivalent

Format ← 1200I

⌈ dyadic

Format 123

SYNTAX ERROR: The function requires a left argument

Format 123

^

Increment ← 10+

⌈ monadic

Windows ← ⊞⊞3

⌈ monadic



What is an operator?

derived
functions

```
4 Increment 2
```

```
SYNTAX ERROR: The function does not take a left argument
```

```
4 Increment 2
```

```
^
```

DYADIC
OPERATOR

```
Replace ← 'Hi ' □ R 'Hello'
```

A ambivalent

```
Increment ← 1 ◦ +
```

A monadic

```
Windows ← ⊖ □ 3
```

A monadic



What is an operator?

| | | FUNCTION | | |
|-----------------------------------|----------------|----------------|---------------|-------------------|
| Γ deriving $a \rightarrow$ | | <i>monadic</i> | <i>dyadic</i> | <i>ambivalent</i> |
| OPERATOR | <i>monadic</i> | + \ | 1200I | 42~ |
| | <i>dyadic</i> | + 3 | + . x | , 2 |



How are they defined/identified?

TRADFN

Calling syntax in header

▽ `res ← x Name y`
`res ← x y`
▽

DFN

Presence of α and ω in body

Name ← {
 α ω
}

dyadic function



How are they defined/identified?

TRADOP

Calling syntax in header

▽ $res \leftarrow (F \text{ Name}) y$
 $res \leftarrow F \ y$
▽

DOP

Presence of $\alpha\alpha$ or $\omega\omega$ in body

Name $\leftarrow \{$
 $\alpha\alpha \ \omega$
 $\}$

monadic operator deriving a monadic function



How are they defined/identified?

TRADOP

Calling syntax in header

▽ $res \leftarrow x(F \text{ Name}) y$
 $res \leftarrow x \ F \ y$
▽

DOP

Presence of $\alpha\alpha$ or $\omega\omega$ in body

Name \leftarrow {
 $\alpha \ \alpha\alpha \ \omega$
}

monadic operator deriving a dyadic function



How are they defined/identified?

TRADOP

Calling syntax in header

▽ $res \leftarrow x(F \text{ Name } G) y$
 $res \leftarrow x \ F \ G \ y$
▽

DOP

Presence of $\alpha\alpha$ or $\omega\omega$ in body

Name \leftarrow {
 $\alpha \ \alpha\alpha \ \omega\omega \ \omega$
 }
}

dyadic operator deriving a dyadic function



How are they defined/identified?

TRADOP

Calling syntax in header

▽ $res \leftarrow (F \text{ Name } G) y$
 $res \leftarrow F \text{ } G \text{ } y$
▽

DOP

Presence of $\alpha\alpha$ or $\omega\omega$ in body

Name $\leftarrow \{$
 $\alpha\alpha \ \omega\omega \ \omega$
}

dyadic operator deriving a monadic function



Apply multiple functions in similar ways

Add a parameter to tweak behaviour

Achieve nicer looking expressions

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Demo: utilities

```
_S ← {α ← ↑ ω (α α α ω)}  A Stack
```

```
Vowel ← ε ◦ 'AEIOU'
```

```
Vowel _S □ A
```

```
'AEIOU' ι _S □ A
```

```
_T ← {α ← ↑ ω (α α α ω) ◊ □ ← α (62 □ ATX 'αα') ω '→' r ◊ r}  A Trace
```

```
-_T / 3 1 4 1 5
```



Demo: combinators/compositions

```
A_ ← {α(ωω αα ωω~)ω}  A Across  
'HELLO' ∘ A_ ~ 'APL'
```

```
_H_ ← {(αα ω)ωω ω}  A Hook
```

```
φ_H_ ≡ ``'hello' 'racecar' 'APL' 'ABBA' 'max'
```

```
φ_H_ ≡ ``_S'hello' 'racecar' 'APL' 'ABBA' 'max'
```

```
φ_H_ ≡ ``_H_/'hello' 'racecar' 'APL' 'ABBA' 'max'
```



Demo: thought concepts

```
A param Fn _W_ Cond initArg
_W_ ← {α ← ⊢ ◊ ω ω ω : α ∇ α α ω ◊ ω}  A While
2 × _W_ {ω < 100} 4
2 × _T_ _W_ {ω < 100} 4

_E_ ← {α ← ⊢ ◊ 0 :: α ω ω ω ◊ α α ω}  A ErrorElse

_O_ ← {r ← ω ◊ (ε r) ← α α "ε r ◊ r}  A Depth 0
(× / ι)_O 4 5 (2 3)
```



Next Webinar

June 23: TBA

Remember: BAA webinars every other week
britishaplassociation.org/webinar-schedule-2022
June 16th, 30th; July 14th, 28th; etc.

More at: apl.wiki/activities

